## GCSE

## Mathematics A

## Mark Schemes for the Components

## January 2010

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# General Certificate of Secondary Education <br> Mathematics A (J512) 

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## J512/01 Paper 1 (Foundation Tier)

| 1 | (a) | 345 | 1 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 115 | 1 |  |
|  | (c) | 84 | 1 |  |
|  | (d) | 18 | 1 |  |
| 2 | (a) | (i) Tonnes | 1 |  |
|  |  | (ii) Metres | 1 |  |
|  |  | (iii) Litres | 1 | Allow kilograms |
|  | (b) | Square metres is area oe | 1 | or 'Sq $m$ is not a length' or 'should be metres/kilometres' etc |
| 3 | (a) | $(1,5)$ | 1 |  |
|  | (b) | $58 \pm 2$ | 2 | 1 for figs 56 to 60 seen |
|  | (c) | $(4.5,2.5)$ marked | 1 |  |
|  | (d) | Parallel line drawn through A | 1 | Any length |
|  | (e) | $(4,0)$ | 1 | Allow ( 8,0 ) or ( $-2,10$ ) |
| 4 | (a) | (i) 27 | 1 |  |
|  |  | (ii) 4, 9, 11, 6 | 2 | 1 for 2 or 3 correct frequencies |
|  | (b) | (i) $10-19$ | 1 |  |
|  |  | (ii) Do not know actual values oe | 1 |  |
| 5 | (a) | 0.5 | 1 |  |
|  | (b) | 0.75 | 1 |  |
|  | (c) | $1 / 4$ or equivalent fraction | 1 |  |
|  | (d) | 30 | 1 |  |


| 6 | (a) | 102 | 4 | B1 for Sam = 36 (/min) <br> B1 for Lizzie $=30(/ \mathrm{min})$ <br> M1 for Total $=$ their $36 \times 2+$ their 30 <br> Or SC2 for 1020 <br> Or SC1 for 170 |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | (i) SK, KS, KK, US, UK and no incorrect entries | 2 | Ignore repeats Allow 1 if 3 correct |
|  |  | (ii) $2 / 6$ oe | 2 | ft their 6 <br> Allow 1 if SS and KK identified or for $2 / n$ with $n>2$ (need not follow from their total) <br> Deduct 1 mark for poor notation (2 in 6, 2 to $6,2: 6$, 2 out of 6 etc) once only in paper |
| 7 | (a) | 7.8 | 1 |  |
|  | (b) | $6<x<7$ | 1 |  |
|  | (c) | 38 www | 3 | B1 for quotient 3 <br> B1 for rem 14 <br> If division done in 2 steps, e.g. 684/2 = 342 then $342 / 9=38$ then mark the $/ 9$ division as above with quotient 3 and remainder 7 <br> If 'chunking' used allow: <br> B2 for (18×) 35 =630, or ( $9 \times$ ) $35=315$ or better <br> Or B1 for $(18 \times) 30=540$ or $(18 \times) 40=$ <br> 720 or $(9 \times) 30=270$ or $(9 \times) 40=360$ |
| 8 | (a) | (i) 20 | 1 |  |
|  |  | (ii) Correct line drawn | 1 |  |
|  | (b) | (i) Two numbers with a product of 24 ( $p \times q$ ) | 1 |  |
|  |  | (ii) Their $2 p+2 q$ | 1 | Must ft from their (b)(i) |
|  | (c) | 4 | 2 | Allow M1 if area and perimeter calculated for any value Or allow SC1 if a rectangle found (e.g. $6 \times 3$ ) |
| 9 | (a) | (i) $4 r$ | 1 |  |
|  |  | (ii) $10 v+6 w$ | 2 | 1 for one term correct seen |
|  | (b) | (i) 5 | 1 |  |
|  |  | (ii) $y=8.5$ oe | 2 | M1 for $10+7$ or 17 seen |
|  |  |  |  |  |


| 10 | (a) | 180 < answer < 360 | 1 | Award 0 for a diagram |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) <br> (c) | $\begin{aligned} & 167^{\circ} \pm 2 \\ & 45^{\circ} \\ & \text { "line" with ("angles" or " } 180^{\prime} \text { ") } \end{aligned}$ | 1 <br> 1 | '180' can be implied by correct answer/working Where totals are given with reasons they must be correct |
| 11 | (a) | 1/15 | 1 | Or 0.066(66..), 0.067 <br> Deduct 1 mark for poor notation ( 1 in 15, 1 to $15,1: 15$, 1 out of 15 etc ) once only in paper |
|  | (b) | 2/5 cao | 2 | B1 for $6 / 15$ oe seen |
| 12 | (a) | Circle radius 3 anywhere on page | 1 | $2.5 \mathrm{~cm} \leq r \leq 3.5 \mathrm{~cm}$ |
|  | (b) | Correct construction $\pm 2 \mathrm{~mm}$ with arcs visible, lines ruled | 3 | B1 for any line correct length $\pm 2 \mathrm{~mm}$ M1 for construction arcs seen Or SC2 for correct triangle no arcs |
| 13 | (a) | -1, 1, , 7 | 2 | Allow 1 for 2 correct |
|  | (b) | Correct ruled line within tolerance from $x=-2$ to $x=6$ | 2 | B1 for any three of their points correctly plotted |
| 14 | (a) | Correct diagram, condone freehand | 2 | Allow 1 for any cuboid correctly drawn -1 if cuboid is 'transparent' and -1 if one extra incorrect line added on the cuboid |
|  | (b) | $\begin{aligned} & 48 \\ & \mathrm{~cm}^{3} \end{aligned}$ | $\begin{aligned} & 2 \\ & 1 \end{aligned}$ | M1 for $2 \times 3 \times 8$ soi <br> If a different cuboid is drawn ft provided method is clear and correct |
| 15 | (a) | 8 | 2 | M1 for $6 \times 4$ or better seen or $\frac{6}{3}$ |
|  | (b) | 1.5 oe | 3 | B1 for $10 x+5$ <br> or $\frac{20}{5}$ <br> M1 for $10 x=20-$ their 5 or better or for their $10 x=20-5$ or better or $2 x=$ their $\frac{20}{5}-1$ or better |


| 16 | (a) | $\frac{13}{50} \times \frac{2}{2}$ soi by $26 / 100$ | 1 | $\text { Or } \frac{13}{50} \times 100 \text { or } \frac{1}{50}=2 \%(\times 13)$ |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | $\begin{aligned} & 35 \% \\ & 30 \% \\ & \frac{13}{50} \frac{90}{300} \frac{7}{20} \text { or } 26 \%, 30 \%, 35 \% \text { oe } \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | From 7/20 <br> From 90/300 |
| 17 | (a) | 5 points correctly plotted | 2 | M1 for 3 points correct |
|  | (b) | Negative | 1 |  |
| 18 | (a) | 6 pack 23p each <br> 10 pack 22p each <br> 10 pack identified (as better value) | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | $\begin{aligned} & \text { Or } 60 \text { cost } £ 13.80 \text { oe } \\ & \text { and } £ 13.20 \\ & \text { Dependent on two correct linked steps } \end{aligned}$ |
|  | (b) | (i) No. Could be 6 and 4 etc | 1 | oe Must be 'numerical' <br> NOT 'There could be more bags' <br> NOT 'We do not know how many bags' |
|  |  | (ii) Bacon: 96 Cheese and onion: 64 | 3 | M1 for $160 \div 5$ soi by 32 <br> A1 for one correct value seen |
| 19 | (a) | 20, 30 | 1,1 | SC1 for reversed answers |
|  | (b) | Complete correct curve from $x=0$ to $x=4$ and above 30 | 2 | $\pm 1 / 2$ small sq for points and curve Daylight above 30 <br> B1 for 4 of their/correct points correctly plotted |
|  | (c) | (i) 30.5 to 32.5 | 1 |  |
|  |  | (ii) 0.5 to 0.9 or their time (at 15) $\pm 0.1$ | 1 | ft is dependent on graph with one solution only between 0 and 4 |
| 20 | (a) | 4 sectors of $96,60,120,84$ <br> 4 labels indicating apple varieties | $3$ | Allow 1 for each correct sector $\pm 2^{\circ}$ to a maximum of 3 marks <br> If $\mathbf{0}$ scored allow $\mathbf{1}$ for $96,60,120,84$ seen |
|  | (b) | (i) 5 correct heights plotted At midpoints and joined | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | $\pm 1 / 2$ small sq <br> Ruled lines. Ignore lines from either end. |
|  |  | (ii) For example: treated trees give more weight | 1 | Or treated have fewer trees with low weights etc |

## J512/02 Paper 2 (Foundation Tier)



| 7 | (a) | 1.2 oe | 1 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 68 | 2 | M1 for $0.17 \times 400$ oe or $1 \%$ is 4 so $17 \%$ is $17 \times 4$ oe |
|  | (c) | 2.272 isw | 2 | M1 for $0.71 \times 3.2$ oe or 2.27 |
| 8 | (a) | (i) 8 | 1 |  |
|  |  | (ii) 31 | 1 |  |
|  | (b) | 22.2 www | 3 | M2 for attempt to find the sum of the scores $\div 10$ Or M1 for attempt to find the sum of the scores |
| 9 | (a) | (i) Odd | 1 |  |
|  |  | (ii) Multiples of 6 or an even number or a multiple of 3 | 1 |  |
|  | (b) | 2.6 | 2 | M1 for $3 \times 4.2+2 \times-5$ or sight of 12.6 or -10 |
| 10 | (a) | 3 correct points $(10,14)(20,28)$ $(40,56)$ <br> Correct ruled straight line through $(10,14)$ and $(40,56)$ | 2 1 | B1 for 1 or 2 correct <br> Ruled straight line going through their 3 points acceptable |
|  | (b) | Answer from their ruled straight line at $x=32$ | 1 |  |
|  | (c) | Answer from their ruled straight line at $y=20$ | 1 | After 0 in (b) and (c), SC1 for answers of (b) 44 to 45 and (c) 14 to 15 |
| 11 | (a) | (i) 38 | 2 | M1 for $180-2 \times 71$ oe or sight of 142 |
|  |  | (ii) Angles in a triangle add up to 180 or base/two angles in an isosceles (triangle) are equal | 1 |  |
|  | (b) | (i) 141 | 2 | M1 for 180 - (180 - (90 + 51)) oe or 39 seen |
|  |  | (ii) Correct explanation for working out angle $y$ | 2 | B2 for an external angle of a triangle is the sum of the opposite two angles Or <br> B1 for angles in a triangle add up to 180 And B1 for angles on a straight line add up to 180 |
|  |  |  |  |  |


| 12 | (a) | (i) $\frac{11}{19}$ isw or $0.57(\ldots)$ or 0.58 | 2 | B1 for $11 / n$ or $n / 19$ or 11 and 19 seen in an answer but not in a ratio |
| :---: | :---: | :---: | :---: | :---: |
|  |  | (ii) $\frac{8}{19}$ isw except do not accept $1 / 2$ or 0.42(...) | 1 | ft their 19 provided answer as fraction |
|  |  | $\text { (iii) } \frac{0}{(19)}$ | 1 | ft their 19 provided answer as fraction |
|  | (b) | Correct explanation as to why the dice is biased | 1 | There are a lot more fours oe or there should be roughly the same of each number oe |
| 13 | (a) | 0.58(...) or 47/81 | 2 | M1 for 4.7/8.1 |
|  | (b) | 2.14(...) | 2 | $\text { M1 for }(\sqrt{ }) 4.59(36) \text { or } \frac{3 \sqrt{319}}{25}$ |
| 14 | (a) | Correct enlargement | 2 | B1 for 1 correct side in an enlarged triangle |
|  | (b) | $\begin{aligned} & 2.16 \\ & 4.14 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  |
|  | (c) | 25 | 2 | M1 for attempting to find 100/4 or $10 / 2 \times 10 / 2$ or sight of $5 \times 5$ oe |
| 15 | (a) | 3.75 or $33 / 4$ or $15 / 4$ | 2 | M1 for $3 / 4 \times(10 / 2)$ |
|  | (b) | 13 www | 3 | M2 for 13.3... <br> or $1500 / 112.5$ and $1000 / 70$ <br> Or M1 for (flour) (figs 1500)/(figs 225) or 6.6(...) <br> or 6.7 or (figs 1500 )/(figs 112.5) <br> or (salt) (figs 1000)/(figs 140) or 7.1(...) <br> or (figs 1000)/(figs 70) |
| 16 |  | ( $6 \times 7=$ ) 42 or 2 tins left each week <br> or $44 / 7=6.2857 \ldots$ or $44 / 6=71 / 3$ <br> $44-42=2$ and $2 \times 21=42$ <br> or $21 \times 44$ or $21 \times 42$ <br> or $0.2857 \ldots \times 21=6$ or $1 / 3 \times 21=7$ <br> After 21 weeks enough (42) left for $22^{\text {nd }}$ week or enough for next 7 days | M1 <br> M1 <br> A1 |  |


| 17 | (a) | Fully correct two-way table with labels cars with numbers at least $1-3$ and people with numbers at least 1 - 5 | 3 | B2 for two-way table with at most one error in missing label or incomplete row of numbers or use of axes <br> Or B1 for two-way table with at most two errors in missing labels or incomplete row of numbers or use of axes |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 14 in correct position on table | 1 |  |
| 18 | (a) | 46 <br> Interior or co-interior or allied or full clear description of interior angles, not just supplementary | $1$ | Allow fully correct alternative with all reasons correct <br> e.g. Opposite angles of parallelogram are equal and angles in quadrilateral/parallelogram add to 360 <br> e.g. Angles on a straight line add to 180 and corresponding angles are equal |
|  | (b) | 35 www | 4 | $\begin{aligned} & \text { M3 for } 5 y=\text { their } 175 \\ & \text { or their } 175 \div 5 \\ & \text { Or M2 for } 5 y+\text { their } 185=360 \\ & \text { or } 5 y \text { and their } 175 \text { seen } \\ & \text { Or M1 for } y+4 y+118+67(=360) \\ & \text { or } 360-(118+67) \end{aligned}$ |
| 19 | (a) | $d^{11}$ | 1 |  |
|  | (b) | $d^{6}$ | 1 |  |
| 20 |  | 240 www | 4 | B3 for 240.1-240.3 <br> Or M2 for $2 \times \pi \times 4.2 \times 9.1$ <br> Or M1 for $2 \times \pi \times 4.2$ or $\pi \times 8.4$ <br> If M0 or M1 or M2 award also B1 for their answer rounded to 2 sig figs <br> If curved surface area calculated plus either one or two circles giving answer in range 295-296 or 350-351 then SC2 plus, if appropriate, B1 for rounding to 2 sig figs, 300 or 350 <br> If $\pi \times 4.2 \times 9.1$ and final answer in range $120-$ 120.09 then SC1 plus, if appropriate, B1 for rounding to 120 |

## J512/03 Paper 3 (Higher Tier)

| 1 | (a) | 0.45 oe | 2 | M1 for $1-(0.05+0.15+0.35)$ |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 0.4(0) oe | 2 | M1 for $0.05+0.35$ or $0.4(0) \div 1$ |
| 2 | (a) | -2 | 2 | M1 for $3 x+2$ or $x+7$ or $2 x-2$ or $-x+5$ seen |
|  | (b) | 8 | 2 | M1 for $6 \times 4$ or better seen or $\frac{6}{3}$ |
|  | (c) | 1.5 oe | 3 | B1 for $10 x+5$ <br> Or $\frac{20}{5}$ <br> M1 for $10 x=20-$ their 5 or better or for their $10 x=20-5$ or better or $2 x=$ their $\frac{20}{5}-1$ or better |
| 3 | (a) | $\frac{13}{50} \times \frac{2}{2}$ soi by $26 / 100$ | 1 | Or $\frac{13}{50} \times 100$ or $\frac{1}{50}=2 \%(\times 13)$ |
|  | (b) | $\begin{aligned} & 35 \% \\ & 30 \% \\ & \frac{13}{50} \frac{90}{300} \frac{7}{20} \text { or } 26 \%, 30 \%, 35 \% \text { oe } \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | From 7/20 <br> From 90/300 |
| 4 | (a) | $4 \mathrm{~cm} \pm 2 \mathrm{~mm}$ line in their kite <br> Both $4.5 \mathrm{~cm} \pm 2 \mathrm{~mm}$ lines in their kite Both $6 \mathrm{~cm} \pm 2 \mathrm{~mm}$ lines in their kite | 1 1 1 | After 0 scored, SC1 for any one correct length $\pm 2 \mathrm{~mm}$ |
|  | (b) | $90-105 \mathrm{~cm}$ | 2 | B1 for length 9 to 10.5 cm seen |
| 5 | (a) | 5 points correctly plotted | 2 | M1 for 3 points correct |
|  | (b) | Negative | 1 |  |
|  | (c) | Line between $(4,21)$ and $(4,23)$ and between $(10,13)$ and $(11,14)$ | 1 |  |
|  | (d) | 17 to 19 | 1 |  |
| 6 | (a) | 6 pack 23p each <br> 10 pack 22p each <br> 10 pack identified (as better value) | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | ```Or 60 cost £13.80 oe and £13.20 Dependent on two correct linked steps``` |
|  | (b) | (i) No. Could be 6 and 4 etc | 1 | oe Must be 'numerical' NOT 'There could be more bags' NOT 'We do not know how many bags' |
|  |  | (ii) Bacon: 96 Cheese and onion: 64 | 3 | M1 for $160 \div 5$ soi by 32 <br> A1 for one correct value seen |


| 7 |  | 4.5 www <br> $\mathrm{g} / \mathrm{cm}^{3}$ or g per $\mathrm{cm}^{3}$ oe | $\begin{aligned} & 3 \\ & 1 \end{aligned}$ | B1 for 30 <br> M1 for $135 \div$ their 30 |
| :---: | :---: | :---: | :---: | :---: |
| 8 | (a) | 5 correct heights plotted <br> At midpoints and joined | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | $\pm 1 / 2$ small sq <br> Ruled lines. Ignore lines from either end. |
|  | (b) | (i) For example: treated trees give more weight | 1 | Or treated have fewer trees with low weights etc |
|  |  | (ii) No (soi). Insufficient information | 1 | Or 'Only total weight recorded' Or 'Do not know how many apples' |
| 9 | (a) | 48,50,56, 60 or 64 www | 2 | M1 for two of 4, 8, 0.5 |
|  | (b) | (i) 5 | 1 |  |
|  |  | (ii) $1 / 8$ or 0.125 | 1 |  |
|  |  | (iii) 1 | 1 |  |
| 10 | (a) | 20, 30 | 1,1 | SC1 for reversed answers |
|  | (b) | Complete correct curve from $x=0$ to $x=4$ and above 30 | 2 | $\pm 1 / 2$ small sq for points and curve <br> Daylight above 30 <br> B1 for 4 of their/correct points correctly plotted |
|  | (c) | (i) 30.5 to 32.5 | 1 |  |
|  |  | (ii) 0.5 to 0.9 or their time at $15 \pm 0.1$ | 1 | ft is dependent on graph with one solution only between 0 and 4 |
|  |  |  |  |  |
| 11 | (a) | 25.5 ( $\times 10$ oe | 1 | Or $25 \times 10+0.5 \times 10$ Condone 25.499(9..) |
|  | (b) | 252.5 | 2 | B1 for 245 or 7.5 seen |
| 12 | (a) | $(x=) \frac{y+2}{3} \text { oe }$ | 2 | M1 for $3 x=y+2$ or $\frac{y}{3}=x-\frac{2}{3}$ or complete reverse flow diagram |
|  | (b) | (i) $\frac{1}{2}$ oe | 2 | M1 for drawing a triangle on the line or (correct diff in $y$ )/( correct diff in $x$ ) |
|  |  | (ii) $y=$ their $\frac{1}{2} x+1$ oe | FT2 | M1 for $y=\frac{1}{2} x+c$ or their $\frac{1}{2} x+1$ |
|  | (c) | $(1 / 2,4)$ oe | 1,1 | After B0, M1 for $\left(\frac{-3+4}{2}, \frac{3+5}{2}\right)$ |
| 13 |  | 400 www | 3 | M2 for $320 \div 0.8$ <br> Or M1 for $0.8 x=320$ oe or $320 \div 80$ |
|  |  |  |  |  |


| 14 |  | $\begin{aligned} & \pi \times 60^{2} \text { or } \pi \times 8^{2} \text { soi } \\ & 3600 \pi \text { or } 64 \pi \\ & (\pi \times) 60^{2}-(\pi \times) 8^{2} \text { oe } \\ & 3536 \pi \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 | After 0 scored, SC1 for any use of $\pi \times r^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 15 | (a) | Complete correct diagram | 2 | B1 for 0.8 correct once |
|  | (b) | 0.64 oe | 2 | M1 for their $0.8 \times$ their 0.8 |
| 16 | (a) | -5 and (+)1 | 1 |  |
|  | (b) | $10 y^{2}+11 y-6$ | 3 | M2 for 3 of $10 y^{2},-4 y,(+) 15 y,-6$ seen Or M1 for 2 of these seen |
| 17 |  | For example: <br> $A B=C D$ <br> $A D=B C$ <br> Opposite sides of a para. are equal <br> $B D$ is common oe <br> (Congruent) SSS | $\begin{aligned} & 1 \\ & 1 \\ & 1 \\ & 1 \\ & 1 \end{aligned}$ | Or SAS or ASA only <br> Any correct reason (dependent on a correct pair identified with letters) $\operatorname{dep} 3^{\text {rd }}$ fact to complete SSS, SAS or ASA <br> Dependent on 3 scored (not reason) |
| 18 | (a) | $y=\frac{36}{x^{2}} \text { oe }$ | 2 | M1 for $y=\frac{k}{x^{2}}$ oe and attempt to subst. |
|  | (b) | 0.36 oe | 1 |  |
|  | (c) | 3, -3 | 1,1 | After 0 scored, SC1 for $x^{2}=9$ |
| 19 | (a) | Area bigger oe | 1 | Eg 'same height, twice/different width' or 'twice the size' 'twice as many students' <br> Soi by 8 and 16 |
|  | (b) | 62 | 3 | B2 for two of 9,39 and 14 www <br> Or B1 for one of 9, 39 and 14 www <br> Or SC2 for figs 62 seen <br> Or SC1 for answer of 31 |
| 20 | (a) | 150 | 1 |  |
|  | (b) | 210 and 330 | 1,1 |  |
| 21 |  | $\begin{aligned} & x^{2}+(x-3)^{2}=17 \\ & x^{2}-3 x-3 x+9 \text { or better } \\ & x^{2}+x^{2}-3 x-3 x+9-17=0 \text { or } \end{aligned}$ better $(2 x-8)(x+1) \text { oe }$ $\begin{aligned} & x=4 \text { and }-1 \\ & y=1 \text { and }-4 \end{aligned}$ | M1 <br> B1 <br> M1 <br> A1 <br> A1 <br> A1 | Or equivalent working in $y$ <br> Collecting their two $x^{2}$ expressions $=0$ $\begin{aligned} & (x-4)(2 x+2) \text { or }(x-4)(x+1) \text { or } \\ & \frac{6 \pm 10}{4} \text { oe } \end{aligned}$ <br> After AOAO, SC1 for one $x$ and its $y$ seen |

## J512/04 Paper 4 (Higher Tier)

| 1 | (a) | 0.58(...) or 47/81 | 2 | M1 for 4.7/8.1 |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 2.14(...) | 2 | $\text { M1 for }(\sqrt{ }) 4.59(36) \text { or } \frac{3 \sqrt{319}}{25}$ |
| 2 | (a) | 3.75 or $33 / 4$ or $15 / 4$ | 2 | M1 for $3 / 4 \times(10 / 2)$ |
|  | (b) | 13 www | 3 | M2 for 13.3... <br> or 1500/112.5 and 1000/70 <br> Or M1 for (flour) (figs 1500)/(figs 225) <br> or $6.6(\ldots$ ) or 6.7 or (figs 1500 )/(figs <br> 112.5) <br> or (salt) (figs 1000)/(figs 140) or 7.1(...) <br> or (figs 1000)/(figs 70) |
| 3 | (a) | (i) Fully correct two-way table with labels cars with numbers at least $1-3$ and people with numbers at least 1 - 5 | 3 | B2 for two-way table with at most one error in missing label or incomplete row of numbers or use of axes Or B1 for two-way table with at most two errors in missing labels or incomplete row of numbers or use of axes |
|  |  | (ii) 14 in correct position on table | 1 |  |
|  | (b) | No box for 3 or rewrite more than 3 as 3 or more | 1 |  |
| 4 | (a) | 46 <br> Interior or co-interior or allied or full clear description of interior angles, not just supplementary | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | Allow fully correct alternative with all reasons correct <br> e.g. Opposite angles of parallelogram are equal and angles in quadrilateral/parallelogram add to 360 e.g. Angles on a straight line add to 180 and corresponding angles are equal |
|  | (b) | 35 www | 4 | M3 for $5 y=$ their 175 or their $175 \div 5$ <br> Or M2 for $5 y+$ their $185=360$ <br> or 5 y and their 175 seen <br> Or M1 for $y+4 y+118+67(=360)$ or $360-(118+67)$ |
| 5 |  | ( $6 \times 7=$ ) 42 or 2 tins left each week or $44 / 7=6.2857 \ldots$ or $44 / 6=71 / 3$ <br> $44-42=2$ and $2 \times 21=42$ <br> or $21 \times 44$ or $21 \times 42$ <br> or $0.2857 \ldots \times 21=6$ or $1 / 3 \times 21=7$ <br> After 21 weeks enough (42) left for $22^{\text {nd }}$ week or enough for next 7 days | M1 <br> M1 <br> A1 |  |


| 6 | (a) | -127 | 2 | B1 for 2 consecutive correct |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | -2 26 in any order | 2 | B1 for numbers that differ by 4 and at least one positive and one negative |
| 7 | (a) | Rotation <br> Centre ( 0,0 ) or origin <br> Angle $90^{\circ}$ (anti-clockwise) or $270^{\circ}$ <br> clockwise or $-270^{\circ}$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | Not turn <br> If combination of two transformations, then SC1 for fully correct descriptions using correct mathematical terminology |
|  | (b) | Fully correct reflection | 2 | B1 for image with 2 correct vertices If B0, then SC1 for reflection shape A in $y$-axis or shape B in $x$-axis or $y$-axis |
| 8 | (a) | 3.42 | 3 | M2 for their $342 \div 100$ <br> Or M1 for 342 or $\Sigma$ at least 4 correct products |
|  | (b) | No, all frequencies close to 100/6 or frequencies nearly all same | 1 |  |
| 9 | (a) | $d^{11}$ | 1 |  |
|  | (b) | $d^{6}$ | 1 |  |
| 10 |  | 240 www | 4 | B3 for 240.1-240.3 <br> Or M2 for $2 \times \pi \times 4.2 \times 9.1$ <br> Or M1 for $2 \times \pi \times 4.2$ or $\pi \times 8.4$ <br> If M0 or M1 or M2 award also B1 for their answer rounded to 2 sig figs <br> If curved surface area calculated plus either one or two circles giving answer in range 295-296 or 350-351 then SC2 plus, if appropriate, B1 for rounding to 2 sig figs, 300 or 350 <br> If $\pi \times 4.2 \times 9.1$ and final answer in range 120-120.09 then SC1 plus, if appropriate, B1 for rounding to 120 |


| 11 | (a) | 2345 | 3 | M2 for $7 / 4<n \leq 5$ or $2 \leq n \leq 5$ <br> or 3 correct values given with no incorrect values <br> Or M1 for either 7/4 or 5 in working or one correct value if only one value stated <br> If MO then SC2 for 2, 3, 4, 5 seen and followed by $8,12,16,20$ <br> Or SC1 for 8, 12, 16, 20 only |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | Fully correct | 3 | B2 for all lines correct and no/incorrect shading <br> Or B1 for two lines correct and no/incorrect shading If B0 then SC1 for lines $x+y=7$ and $x=3$ and $y=2$ |
| 12 |  | $5.7^{2}+12.9^{2}$ or 198.9 or 199 <br> $14.4^{2}=207.36$ or $\sqrt{ } 198.9=14.1(\ldots)$ <br> No, answers not equal or $14.1 \neq 14.4$ | M1 <br> M1 <br> A1 | For full alternative explanations <br> M2 for finding both smaller angles or one smaller angle using two or more trig ratios <br> Or M1 followed by M1 for method to find largest angle e.g. cosine rule |
| 13 |  | $y=86$ <br> Angle at centre double angle at circumference $z=137$ <br> Sum opposite angles cyclic quadrilateral 180 | $\begin{aligned} & 1 \\ & 1 \\ & 1 \\ & 1 \end{aligned}$ |  |
| 14 |  | $\begin{aligned} & 3(x) \text { and } 5(x) \text { seen/used } \\ & 8 x \times 5 x(=810) \\ & \text { their } 40 x^{2}=810 \\ & x^{2}=810 / \text { their }(8 \times 5) \text { or } x^{2}=\text { their } 20.25 \\ & 4.5 \mathrm{www} \end{aligned}$ | M1 <br> M1 <br> M1 <br> M1 <br> A1 | $3^{\text {rd }} \mathbf{~ M 1 ~ d e p ~ o n ~} 1^{\text {st }} \mathbf{~ M} \mathbf{1}$ <br> 4th M1 dep on $3^{\text {rd }} \mathbf{M 1}$ <br> If no working, then SC4 for 4.5 |
| 15 | (a) | Points plotted correctly $\pm 1 / 2$ small square and joined to form line/curve | 3 | If $\mathbf{0}$ then $\mathbf{B 1}$ for $\geq 7$ plots (excluding ( 0,0 )) at upper bound and B1 for $\geq 7$ plots (excluding $(0,0)$ ) at correct height |
|  | (b) | German and 5.5-8 marks | 2 | B1 for difference medians 5.5-8 |
| 16 | (a) | (i) $x(x-8)$ | 1 |  |
|  |  | (ii) $2 x\left(3 x^{2}+5 y^{3}\right)$ | 2 | M1 for $2\left(3 x^{3}+5 x y^{3}\right)$ or $x\left(6 x^{2}+10 y^{3}\right)$ |
|  |  | (iii) $(2 x-y)(2 x+y)$ | 2 | M1 for $(2 x-y)$ or $(2 x+y)$ as part of product |
|  | (b) | $\frac{x+3}{3 x} \text { or } \frac{1}{3}+\frac{1}{x}$ | 2 | M1 for $x(x+3) / 3 x^{2}$ |
|  |  |  |  |  |


| 17 | (a) | $9.1 \times 10^{7}$ | 1 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (b) | 1000 or $10^{3}$ | 2 | M1 for $10^{-9} \div 10^{-12}$ |
| 18 | (a) | $13.3-13.4$ www | 3 | M2 for (QT =) $16.7 \times \sin 53$ oe Or M1 for $\sin 53=$ QT/16.7 oe |
|  | (b) | 36.9(...) www | 3 | M2 for $\cos$ RST $=0.799-0.8$ Or M1 for ( $\cos$ RST $=$ ) $\frac{27.4^{2}+19.1^{2}-16.7^{2}}{2 \times 27.4 \times 19.1}$ |
| 19 | (a) | Exams twice per year | 1 |  |
|  | (b) | $\begin{aligned} & 3800-4000 \\ & 4900-5300 \end{aligned}$ | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | Predicted next moving average stated M1 for $1 / 2(2700+x)=$ their reading oe |
| 20 |  | Trial $\geq 1.5$ and $<2$ and outcome Improved trial and outcome <br> Two correct trials between 1.685 and 1.695 inclusive that give answers below 27 and above 27 Or 1.69 and 1.7(0) with an explanation i.e. working that 1.69 gives a closer answer than 1.7(0) <br> 1.69 | M1 <br> M1 <br> A1 <br> A1 | Improved trial means a further trial which would give an answer closer to 27 <br> Dependent on both M marks only |
| 21 | (a) | $3 \sqrt{ } 5$ | 1 |  |
|  | (b) | $3 \sqrt{6 / 2}$ | 2 | M1 for $9 \sqrt{ } 6 / \sqrt{ } 6 \sqrt{ } 6$ or $9 \sqrt{ } 6 / 6$ |
| 22 | (a) | (i) a | 1 |  |
|  |  | (ii) $\mathbf{a}+\mathbf{b}$ | 1 |  |
|  | (b) | $1 / 3(\mathbf{b}-2 \mathbf{a})$ or $\mathbf{b} / 3-2 \mathbf{a} / 3$ | 3 | B2 for correct unsimplified expression Or M1 for $1 / 3$ their DB or $2 / 3$ their DB seen |
| 23 | (a) | Square numbers always positive When $x=y,(x-y)^{2}=0$ | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ |  |
|  | (b) | $x^{2}-2 x y+y^{2} \geq 0$ and $x^{2}+y^{2} \geq 2 x y$ | 1 |  |

## Grade Thresholds

General Certificate of Secondary Education
Mathematics A (J512)
January 2010 Examination Series

## Component Threshold Marks

| Component | Max Mark | A | B | C | D | E | F | G |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 100 |  |  | 66 | 55 | 44 | 33 | 22 |
| 2 | 100 |  |  | 67 | 56 | 46 | 36 | 26 |
| 3 | 100 | 66 | 49 | 32 | 18 |  |  |  |
| 4 | 100 | 56 | 39 | 23 | 14 |  |  |  |

## Specification Options

Foundation Tier

|  | Max Mark | A* | A | B | C | D | E | F | G |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall Threshold Marks | 200 |  |  |  | 133 | 111 | 90 | 69 | 48 |
| Percentage in Grade |  |  |  |  | 40.9 | 21.6 | 13.7 | 10.2 | 7.3 |
| Cumulative Percentage in <br> Grade |  |  |  |  | 40.9 | 62.5 | 76.2 | 86.4 | 93.7 |

The total entry for the examination was 16286.

Higher Tier

|  | Max Mark | A* | A | B | C | D | E | F | G |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall Threshold Marks | 200 | 156 | 122 | 88 | 55 | 32 | 20 |  |  |
| Percentage in Grade |  | 8.3 | 15.4 | 25.3 | 30.2 | 15.0 | 4.1 |  |  |
| Cumulative Percentage in <br> Grade |  | 8.3 | 23.7 | 49.0 | 79.2 | 94.2 | 98.3 |  |  |

The total entry for the examination was 3462 .

Overall

|  | A* | A | B | C | D | E | F | G |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Percentage in Grade | 1.5 | 2.7 | 4.4 | 39.1 | 20.4 | 12.0 | 8.4 | 6.0 |
| Cumulative Percentage in <br> Grade | 1.5 | 4.2 | 8.6 | 47.7 | 68.1 | 80.1 | 88.5 | 94.5 |

The total entry for the examination was 19748.
Statistics are correct at the time of publication.

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